

EXPERIMENT NUMBER	NEUTRON ABSORBER ⁽⁴⁾ / POSITION IN LATTICE ⁽¹⁾	ARRAY WIDTH (PINS)	CRITICAL LENGTH ^{(2) (5)} (PINS)
013	NONE / ---	15	13.11
014	Cd / ROW 1 (EDGE)	14	15.26
015	BORAL / ROW 1 (EDGE)	14	15.77
041	Gd / ROW 1 (EDGE)	14	15.22
016	Cd / ROW 8 (MIDDLE)	14	21.94
020	BORAL / ROW 8 (MIDDLE)	14	28.29
042	Gd / ROW 8 (MIDDLE)	14	20.91
040	Gd / Gd PINS CENTERED IN 5 x 5 FUEL CLUSTERS ⁽³⁾	15	15.93

- (1) "ROW" REFERS TO LINE OF LATTICE HOLES RUNNING PARALLEL TO LONG SIDE OF TEMPLATES. (SEE FIGURE 2). THE "EDGE" ROW MEANS THE ROW OF TEMPLATE HOLES NORMALLY OCCUPIED BY THE FIRST ROW OF FUEL. THE MIDDLE ROW, LIKewise, REFERS TO THE ROW OF HOLES IN THE ARRAY CENTER.
- (2) THE CORRECT INTERPRETATION OF THE CRITICAL LENGTH IS TO ASSUME THIS AS A FRACTION OF A FULL CELL ALONG THE ENTIRE ARRAY WIDTH. FOR EXAMPLE, IF THE ARRAY LENGTH IS 13.11 ROWS THIS IS 13 ROWS PLUS 0.11 ROWS. DO NOT EQUATE THIS WITH NUMBER OF PINS IN A ROW, OR THE POSITION OF THESE PINS IN THE FRACTIONAL ROW.
- (3) A Gd PIN IS POSITIONED AT THE CENTRAL POSITION OF EVERY 5x5 CLUSTER OF FUEL. THE ENTIRE ARRAY, IN TURN, IS PUT TOGETHER IN A REPETITIOUS MANNER, OF THESE 5x5 CELLS.
- (4) THE BORAL AND Cd PLATES STRETCHED TO THE EDGE OF THE FULL 508 mm TEMPLATE LENGTH. CONSEQUENTLY, SOME PORTION OF THE PLATE WAS OUT IN THE WATER REFLECTOR REGION. THE Gd PINS, HOWEVER, DID NOT EXTEND OUT INTO THE WATER BEYOND THE FUEL.
- (5) THE EXPERIMENT ERROR IS $\leq 0.3\%$ IN CRITICAL LENGTH.

Fig 3 Critical array size for 15 39-mm lattice for various neutron absorber positions in fuel array

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5. Critical Experiments Using High-Enriched Uranyl Nitrate with Cadmium Absorber, W. E. Converse, R. C. Lloyd, E. D. Clayton (BNWL), W. A. Yuill (Allied Chem)

The need for experimental criticality data on high-enriched uranium solution systems containing soluble neutron poisons has been indicated¹ Data have been presented previously on soluble poisons in plutonium systems²⁻⁴ and in low-enriched uranium systems⁵ To supply data required on high-enriched uranium, a series of experiments was performed at the Pacific Northwest Laboratory (Critical Mass Laboratory) using high-enriched (~85 wt% ²³⁵U) uranyl nitrate solution with cadmium nitrate as a soluble neutron

poison These experiments were specifically undertaken to support the design of the dissolvers to be used in the Flourinel Dissolver Process and Fuels Storage (FAST) Facility at the Idaho Chemical Programs Plant (ICPP). The ICPP is operated by the Allied Chemical Corporation, Idaho Chemical Programs, for the U.S. Department of Energy. The experiments supply data for use in criticality safety and as benchmarks to test calculational techniques

This series of experiments was performed using a 241 8-mm-i.d stainless-steel (Type 304) cylindrical vessel reflected on the sides and bottom with at least 200 mm of water or water plus cadmium nitrate The experimental vessel thickness was 0.79 mm on the sides and 6 35 mm on the top and bottom. The cylindrical reflector tank was made of carbon steel with a 1016-mm o d and 2 77-mm-thick walls on the sides and bottom. For all experiments, the reflector solution height was maintained at the top of the experimental vessel. A detailed description of the experimental assembly is shown in Fig. 1.

The uranyl nitrate used in these experiments contained ~500.0 g U/litre with 0 1 M excess nitric acid. The average enrichment was ~85 wt% ²³⁵U

Each experiment was performed by incrementally increasing the uranium solution level in the experimental vessel until the critical level was determined. A safety and

DIMENSIONS OF EXPERIMENTAL VESSEL:

Inside Radius, mm	120.9
Inside Height, mm	1066.8
Side Wall Thickness, mm	0.79
End Thicknesses, mm	6.35

EXPERIMENTAL DIAGRAM:

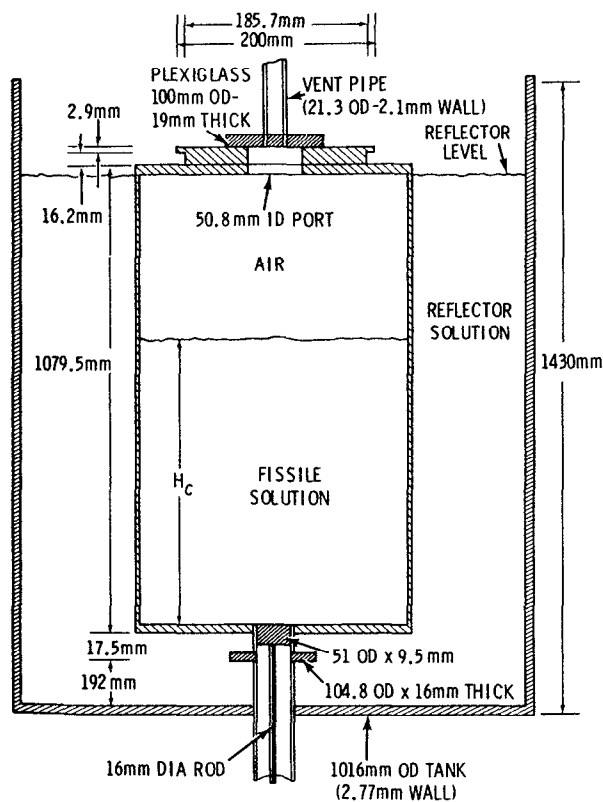


Fig 1. Description of experiment

control rod (positioned external to the experimental tank) were used. At each solution level, the safety rod was fully withdrawn and the control rod was withdrawn until it no longer influenced the reactivity of the experiment. The first two experiments were done with no cadmium added to the uranyl nitrate. The first experiment had water only in the reflector tank and the second had water plus cadmium nitrate (at ~15 g Cd/litre) in the reflector tank. For the remaining experiments, water alone was used in the reflector tank and the cadmium concentration in the uranyl nitrate to the experimental vessel was varied. The results of the experiments including details of solution concentrations and critical solution heights are presented in Table I.

Calculations were performed for each experiment by modeling the system using the KENO-IV⁶ computer code. Cross sections for KENO were generated using the EGGNIT⁷ computer code. Seventeen epithermal- and one thermal-group cross sections were used.⁸ Input data for EGGNIT was FLANGE⁹-ETOG¹⁰-processed ENDF/B-IV data. The calculated k_{eff} 's are also shown on Table I. For unpoisoned cases the codes are calculating about 3% high in k_{eff} . For poisoned cases the codes calculate k_{eff} about 2% low.

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TABLE I

Results of Experiments on the 241 8-mm-i d Cylindrical Vessel Containing Highly Enriched Uranyl Nitrate* and Cadmium Nitrate

Solution Cd ^a Concentration (g Cd/litre)	Reflector Cd ^a Concentration (g Cd/litre)	Critical Height (cm)	Calculations KENO/EGGNIT ^b $k_{eff} \pm 1\sigma$
0	0	22.33	1.024 \pm 0.008
0	15	30.58	1.040 \pm 0.010
1.98	0	28.20	0.971 \pm 0.010
3.98	0	37.75	0.998 \pm 0.012
6.35	0	76.05	0.985 \pm 0.007

*As uranyl nitrate, $UO_2(NO_3)_2$, 478.7 g U/litre, S.G. = 1.6592, 0.194 M excess nitrate. Isotopics (wt%) = $^{234}U = 0.94$, $^{235}U = 85.02$, $^{236}U = 3.46$, $^{238}U = 10.58$

^aAs cadmium nitrate, $Cd(NO_3)_2 \cdot 4H_2O$

^bKENO-IV calculations using 18-group-averaged cross sections from EGGNIT. One sigma (1σ) values are derived from KENO code statistics.

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6. Reactivity Effects due to Spherical Fuel Particles in Uranium-Water Systems, T. J. Trapp, J. P. McNece, D. R. Oden (BNWL)

It is a well-known fact that the maximum reactivity (k_{∞}) attainable in a homogeneous fuel-moderator mixture can increase when the fuel is lumped. A familiar illustration of this effect is the observed difference in the minimum critical enrichments for homogeneous (~ 1 wt% ^{235}U) and heterogeneous (natural U) uranium-water mixtures.¹ There are many computational methods and considerable experimental data available to the criticality safety analyst to allow the evaluation of the safety of either homogeneous fuel-moderator mixtures or lattices of fuel rods immersed in a moderator. However, the analyst is sometimes faced with the practical problem of evaluating an "intermediate" case consisting of a mixture of fuel particles in a moderator. Both the absence of experimental data and the lack of simple computational methods to address this specific problem have led us to develop a computational model for this type of system. This paper presents the results of a series of survey calculations performed using the model to examine the reactivity effects of spherical uranium fuel particles in a water moderator. The computational model is described in a companion paper.² Some of the variables considered in the survey, in addition to spherical particle diameter, include fuel material form (metal, oxide), uranium enrichment, and particle volume fraction (degree of moderation)

Reactivity changes from lumping fuel into particles result from two primary effects. The first effect is that a larger fraction of the neutrons is slowed down in the moderator, thus escaping resonance capture in ^{238}U . This increases the reactivity of the system. The second effect is that neutrons that slow down in the moderator travel some distance in the moderator before encountering a fuel particle. Therefore, a larger fraction of the neutrons is absorbed in the moderator in the heterogeneous mixture than in the homogeneous system. This effect produces changes in the thermal utilization and tends to decrease reactivity.

Modified versions of the GRANIT³ and EGGNIT⁴ computer codes were used to calculate the thermal and epithermal parameters and k_{∞} . The epithermal resonance calculation in EGGNIT was done using integral transport theory.⁵ The thermal calculation in GRANIT was also done using an integral transport theory⁶ method. k_{∞} was calculated based on two-group parameters from a 30-thermal-group and 68-epithermal-group spectrum. In both the thermal and epithermal calculations a Dancoff factor is required for the

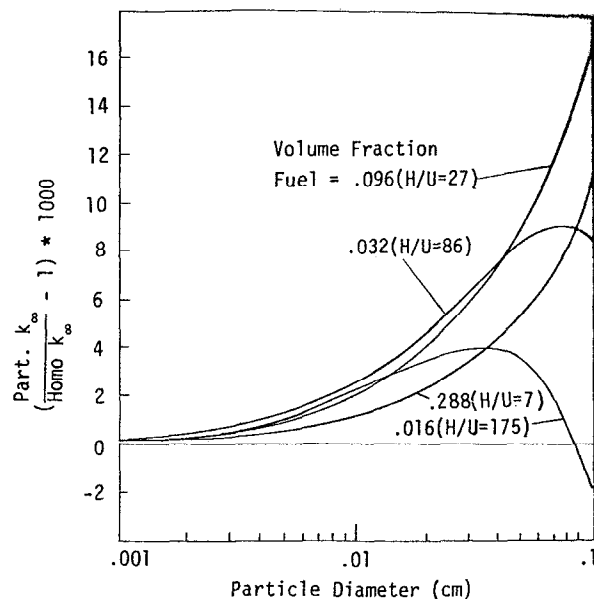


Fig. 1 The ratio of the heterogeneous k_{∞} to the homogeneous k_{∞} for a solution of 5 wt% enriched UO_2 spherical particles in water.

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Figure 1 shows the effects of fuel particle sizes on k_{∞} for 5 wt% enriched UO_2 particles in water. The fractional change ($\times 1000$) in the heterogeneous k_{∞} from the homogeneous k_{∞} is displayed as a function of the particle size. Each curve on the graph corresponds to a system with a fixed volume fraction of uranium (and fixed H/U). The maximum reactivity changes occur with a volume fraction of uranium of ~ 0.1 .

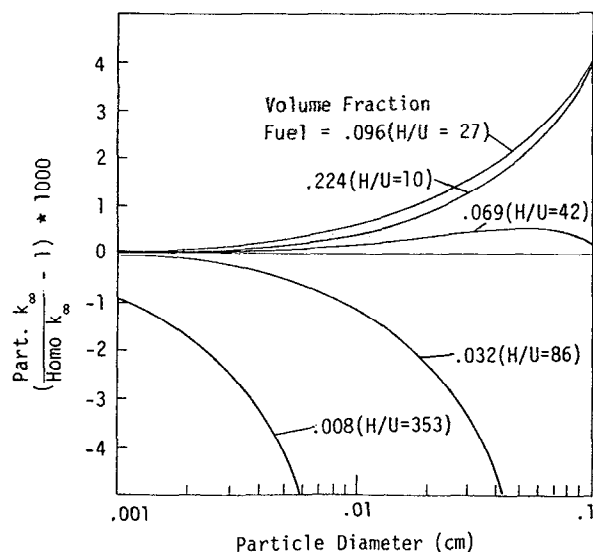


Fig. 2 The ratio of the heterogeneous k_{∞} to the homogeneous k_{∞} for a solution of 95 wt% enriched UO_2 spherical particles in water.

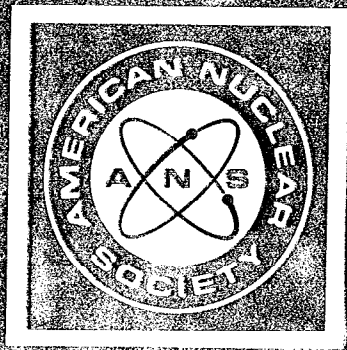
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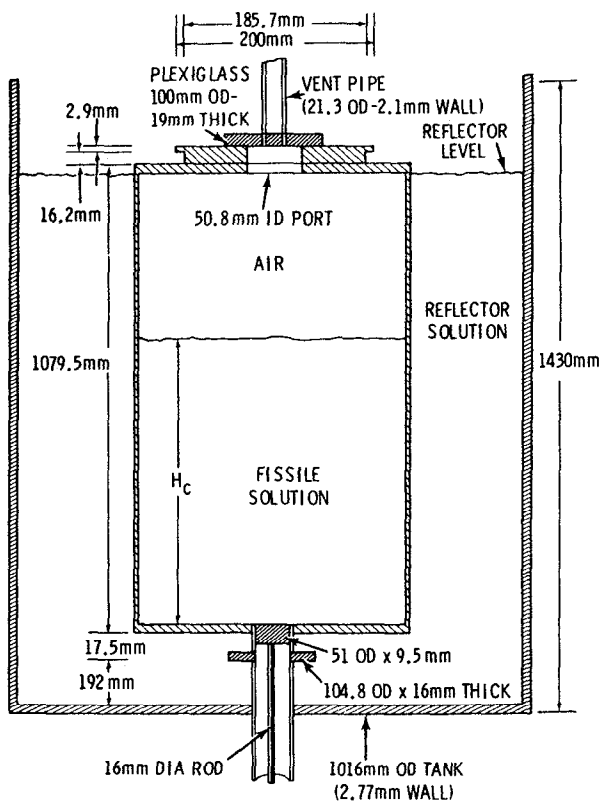


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TABLE I

Results of Experiments on the 241.8-mm-i.d. Cylindrical Vessel Containing Highly Enriched Uranyl Nitrate* and Cadmium Nitrate

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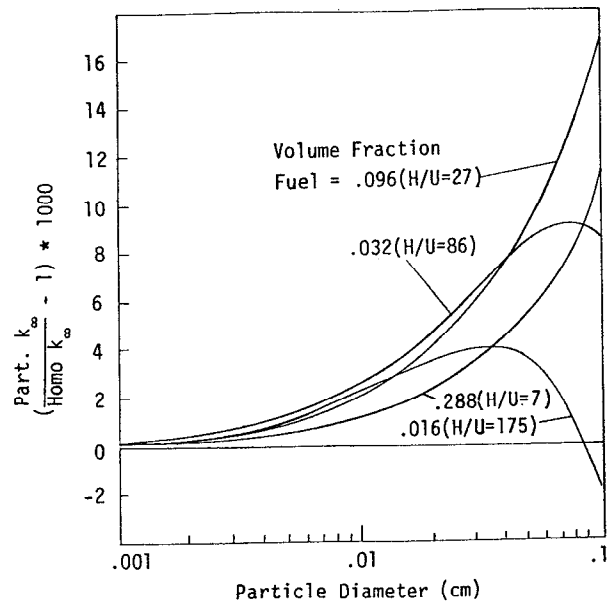


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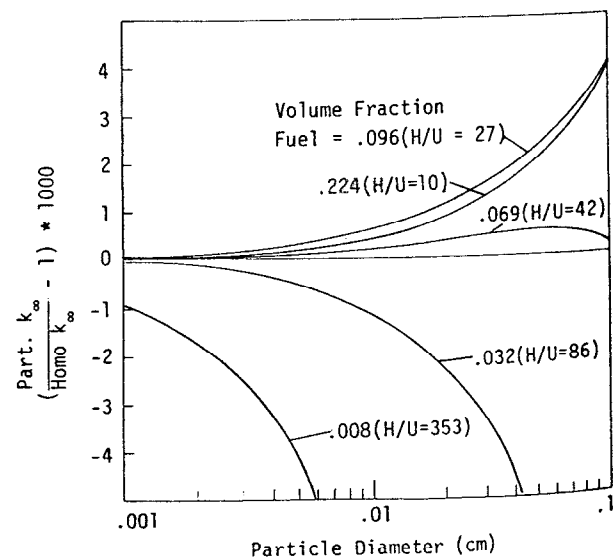


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